

average depression depths should be chosen as geometric parameters of the cross-section of full penetration welds. In our study, h , b , h_b and b_b have been selected to characterize the full penetration weld (cross-section).

Experiments

The primary objective of this paper is to determine the relationship between b_b and the weld-face geometric parameters. At present, it is nearly impossible to exactly obtain this relationship theoretically due to the problem's complexity. Thus, the statistical approaches are adopted.

Data pairs of the weld-face and root-surface geometric parameters are produced by experiments (rather than simulation) in order to perform the statistical analysis. Since the variation in the state of full penetration is caused primarily by the perturbations in welding conditions during actual welding, the relationship must be valid under a wide variety of welding conditions. This implies the experiments must also be performed under a wide variety of welding conditions. The following problems are considered:

1) Root opening: In general, small root openings between two thin plates to be joined are assumed during actual welding. Thus, in our butt joint experiments, the natural root openings are frequently adopted. Here, natural root opening means that the two plates are directly placed together without any additional machining after the plates are cut. In a test piece using the natural root opening, the actual opening measure-

ment varies between 0 to 0.5 mm, randomly. An experiment using gradually varying root openings was also completed.

2) Geometry of the electrode tip: Various electrode tip angles were studied. The electrode tip angles varied from 45 to 60 deg.

3) Material and dimension of test pieces: Stainless steel (18Cr-9Ni-Ti) plates 3 mm in thickness with dimensions as shown in Fig. 3A are utilized. However, a test piece of the same material with the same thickness but dimensions as shown in Fig. 3B is employed to emulate the variation in heat transfer condition.

4) Rate of argon flow: In most experiments, the rates are chosen to be 10L/min, with the single exception of 5L/min.

Based on the previous consideration, five experiments were performed — Table 1. The travel velocity of the welding torch was 2 mm/s. Also, in each experiment, varying current and arc length were utilized.

The geometric parameters h , b , h_b and b_b are measured off-line. In order

to measure these parameters, a He-Ni laser plane, produced by a 2 MW He-Ne laser and a cylindrical lens, is projected on the surface of the test piece to produce either the weld-face or the root-surface curve of the cross-section — Fig. 2. As a result, a digital weld image (Fig. 4A) with laser stripe can be obtained by a camera and an image interface. The image is processed by the following: 1) extracting the medial axis of the laser stripe, which can be regarded as the thinned laser stripe (Ref. 15); 2) recognizing the feature points a and b ; and 3) modeling the medial axis and computing the geometric parameters. The results of the three above steps are illustrated in Fig. 4 and the corresponding details are discussed in Ref. 15.

Figure 5 shows the measured geometrical parameters. The horizontal coordinate is the sampling instant. Each sampling instant corresponds to a distance of 2 mm along the weld bead. In this 2-mm distance, the weld images are sampled and processed three times. The geometric parameters at each sampling instant are the means of the results obtained at these three times.

Table 1 — Experimental Items

No.	Welding Conditions
1	Natural root opening, butt joint, flow rate 10 L/min
2	Natural root opening, butt joint, flow rate 10 L/min
3	Natural root opening, butt joint, argon flow rate changes from 10 to 5 L/min midway
4	Varying root opening, butt joint, 10 L/min, root opening varies from 0 to 0.5 mm gradually
5	Bead-on-plate, varying heat transfer condition, flow rate 10 L/min

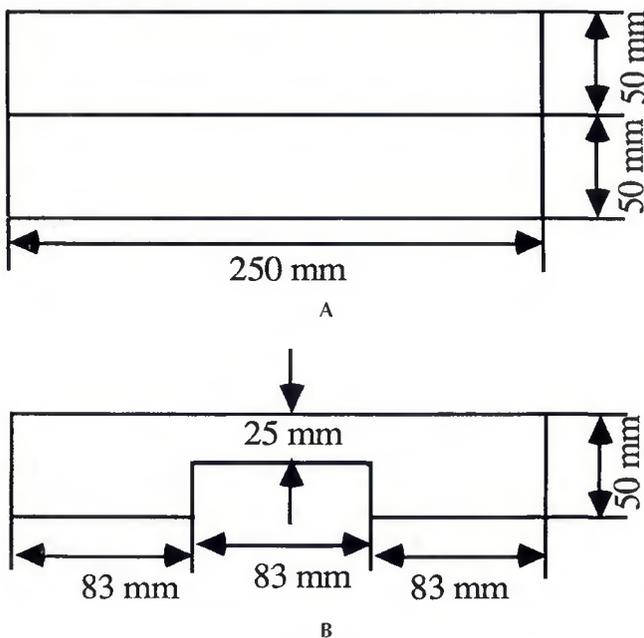


Fig. 3 — Dimensions of the test pieces. A — for butt joint; B — for bead-on-plate.

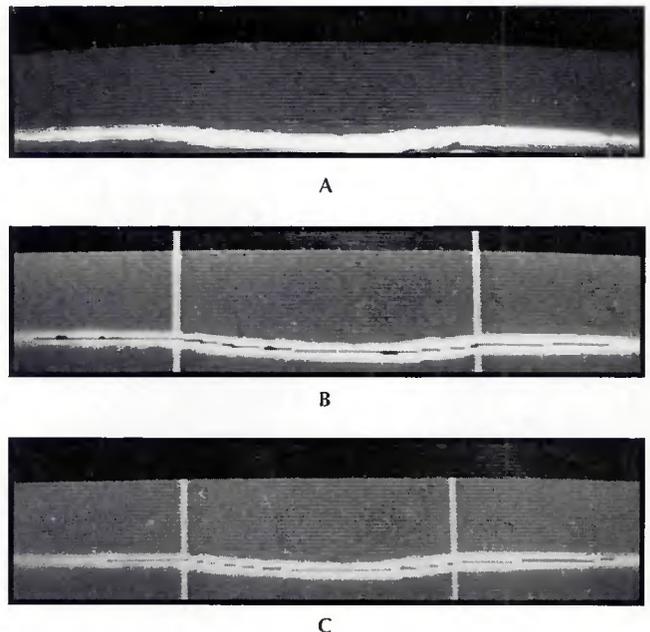
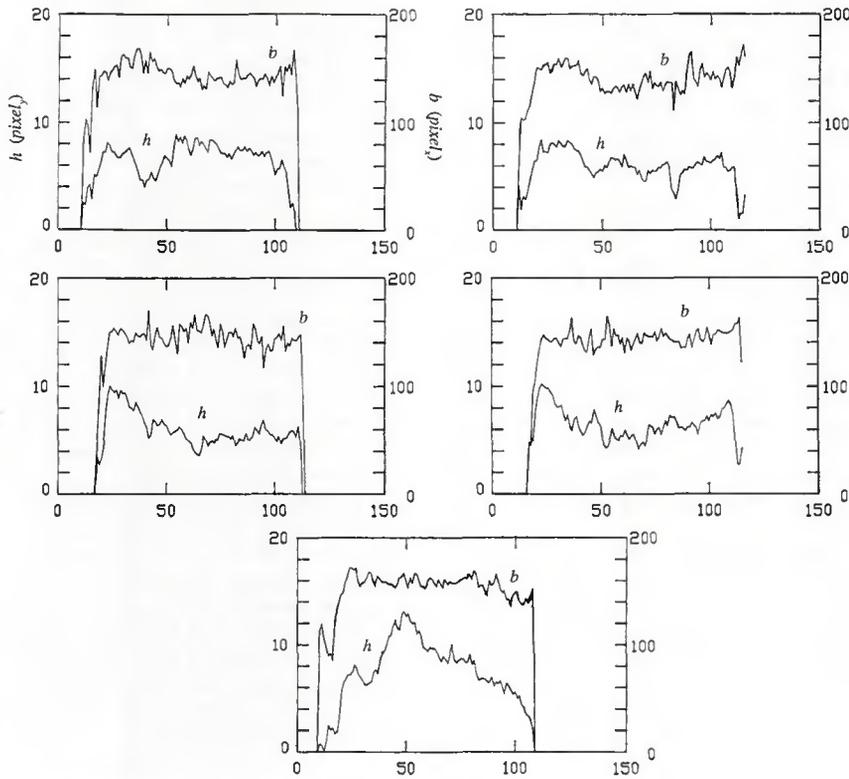
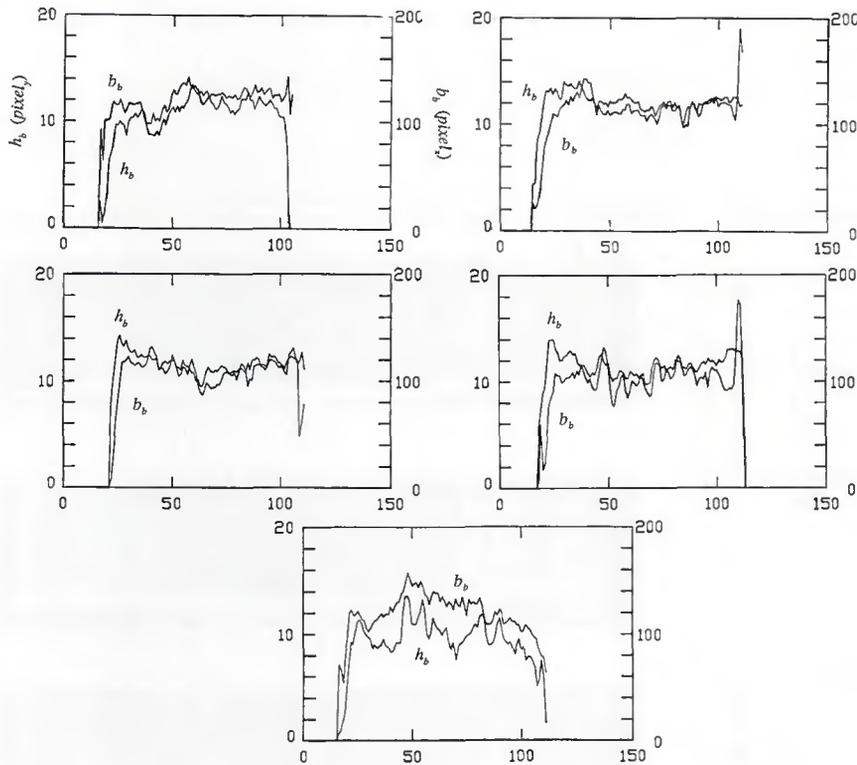


Fig. 4 — Weld-stripe image processing. A — original image; B — medial axis and feature points; C — modeled medial axis.



A



B

Fig. 5 — Measured weld geometric parameters. A — weld-face measurements; B — root-surface measurements.

Statistical Analysis

Let us consider the following linear model (Ref. 18):

$$b_b(k) = \alpha_0 + \sum_{j=1}^n \alpha_j \chi_j(k) = \varepsilon(k) \quad (1)$$

where k is the sampling instant, α_j 's ($j = 0, 1, \dots, n$) are the model parameters to be estimated, $n + 1$ is the number of model parameters, χ_j 's ($j = 1, \dots, n$) are the regressive factors, which consist of the possible function of the weld-face geometric parameters, and $\{\varepsilon(k)\}$ is a white noise sequence representing the modeling error. The following χ_j are proposed: $b, h, bh, b^2, h^2, b^2h^2, \sqrt{b}, \sqrt{h}$, and \sqrt{hb} . The least squares method (Ref. 18) is utilized to estimate the parameters α_j in Equation 1. The procedure of structure determination (i.e., how to choose the regressive factors) is based on the F-test and experience. The final decision on the model structure is made on basis of the F-test results and on model accuracy specifications.

Let

$$\chi(k) = (1, \chi_1(k), \dots, \chi_n(k))^T \quad (2)$$

$$\alpha = (\alpha_0, \alpha_1, \dots, \alpha_n)^T \quad (3)$$

$$\Phi = (\chi(1), \dots, \chi(N))^T \quad (4)$$

$$B_b = (b_b(1), \dots, b_b(N))^T \quad (5)$$

where N is the sample size. The least-squares estimate of α is (Ref. 18):

$$\hat{\alpha}_{LS} = (\Phi^T \Phi)^{-1} \Phi^T B_b \quad (6)$$

In our statistical analysis, data with respect to the beginning and ending portions of weld path is not considered. Seventy data pairs are taken from each test piece. Thus, the sample size is 350 (i.e., $N = 350$).

Initially, models with a single regressive factor are estimated as shown below

Regressive Factor	$\hat{\sigma}^2$ (pixel _x ²)
b	10.6 ²
h	6.23 ²
bh	6.82 ²

where $\hat{\sigma}^2 = J/N$ is the estimate of the variance of ε (J is the residual squares sums) and $\text{pixel}_x = 0.05 \text{ mm}$ — Fig. 5. It is apparent from the variance of ε that the regressive factor h is the best choice.

depression area S . In this case, an increment in b_b appears to be reasonable.

If $S = hb$ remains unchanged, a decrease of h can be caused by an increase in b . The degree of the depression will be decreased. In this case, a decrease in b_b seems reasonable. If S increases more rapidly than b , b_b will increase.

Model Validity

Generally, the validity of an empirical model established utilizing experimental data is correlated to the experimental conditions. If a model is generated based on experiments with a constant current, this model will probably not be valid under a different value of the current or changing current. The experimental conditions involved must produce some restrictions on the possible application cases of the model. To decrease the restriction caused by the experimental condition as much as possible, numerous variations of welding parameters should be employed for the experiments. However, for a specific problem, the fundamental requirements on variations of welding parameters can be determined by case analysis. In our case, the material and plate thickness are not changed. Our model in Equation 7 will be valid for the full penetration GTA welding on 3-mm stainless steel plates (18Cr-9Ni-Ti) even though the variations in current, arc length, electrode tip angle, rate of gas flow, and root opening may exist.

In our experiments, the variations of welding parameters fall into some specific ranges. For example, the variation ranges of current and arc length are (105 A, 135 A) and (1 mm, 5 mm), respectively. In our case, full joint penetration may not be generated if the current is less than 105 A and the arc length is larger than 5 mm. Also, the plates may be melted through with a current larger than 135A and an arc length shorter than 1 mm. Thus, the corresponding weld geometrical parameters will fall into some ranges. When the empirical model is applied, the geometrical parameters must be within the respective ranges used in the model establishment. The distribution of geometrical parameters employed in model development in this study is illustrated in Fig. 9. The experimental data is uniformly distributed in the area $abcd$. This area covers the ranges of possible weld-face weld geometry during closed-loop control of full penetration in our study. Thus, our model is valid for the closed-loop control of full penetration GTA welding, which maintains the weld-face weld parameters within small ranges inside the area $abcd$ to acquire a required root-surface weld width.

Weld Face Supervision Parameters

From Equation 7, we note that the weld-face average depression depth h can sufficiently represent the root-surface weld width. Thus, the weld-face average depression depth may be chosen as the weld-face supervision parameter of the full penetration state. However, the uniform weld-face weld width b should be, in general, obtained during actual welding. Accordingly, both the weld face average depression depth h

and the weld-face weld width b should be controlled. Therefore, h as well as b are chosen to be the weld-face supervision parameters of the full penetration state during the actual control.

Conclusions

The average depression depth is proposed to be a geometric parameter of the cross-section of full joint penetration welds. A linear relationship exists between the full penetration state (the root

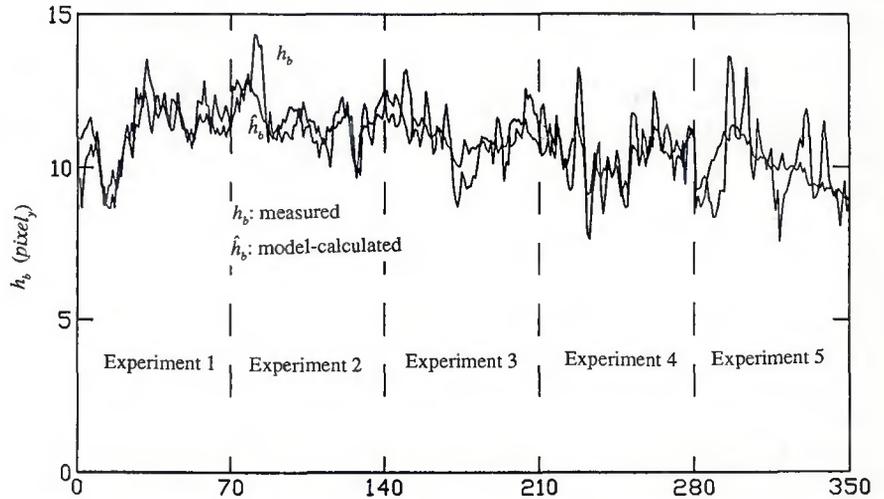


Fig. 8 — Comparison between the measured and model-calculated h_b (individual models).

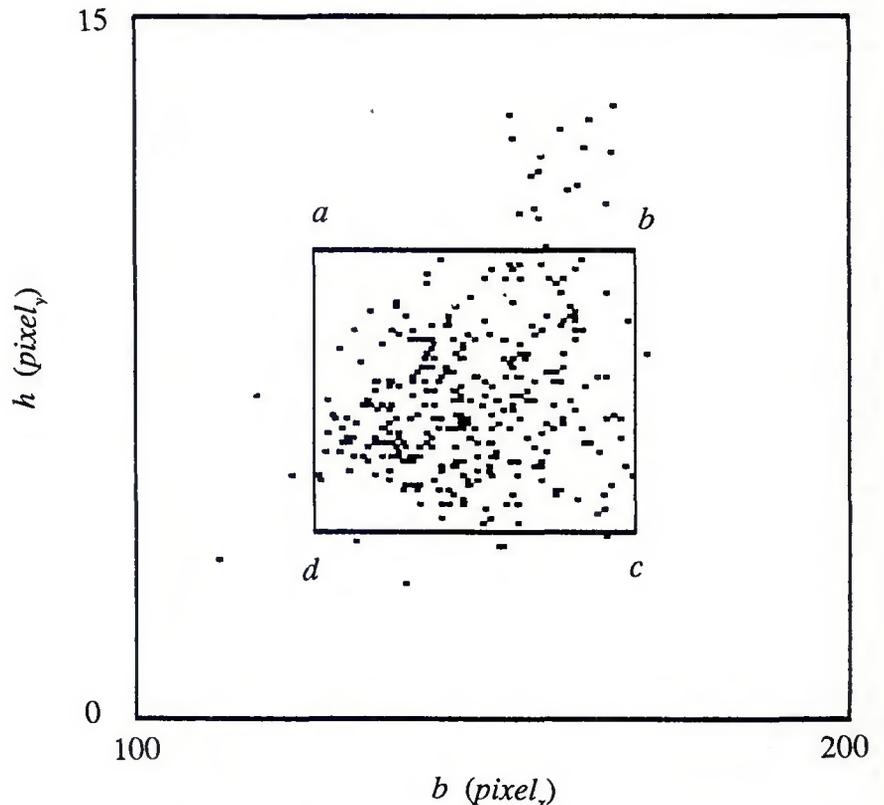


Fig. 9 — Experimental data distribution.

surface weld width) and the weld-face average depression depth. This relationship is obtained by statistical analysis of experimental data. The experiments are performed on stainless steel plates 3 mm in thickness using GTA welding. In order to ensure the validity of the relationship, the experiments have been arranged based on the particular application. The variance of the error of the relationship is 0.312 mm^2 .

Due to the aforementioned relationship, the control of the root-surface weld width may be realized by adjusting the weld-face average depression depth. Based on this concept, a weld-face vision control strategy for the state of full penetration is developed. This novel strategy has been both verified and realized (Refs. 16, 17).

During actual welding, the weld-face weld width needs to be controlled in order to obtain a uniform weld. Thus, both the weld-face average depression depth and the weld-face weld width are taken as the weld-face supervision parameters (outputs) of our full penetration control system.

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