

where $F_s(T)$ is the local solid fraction, T_l is the liquidus temperature and T_s is the solidus temperature. The F_s is calculated based on a sigmoidal function as shown in Ref. 15.

The flow in the mushy zone is assumed to follow the Darcy law (Ref. 22) given by,

$$u = -(K/\mu) \nabla P$$

where K is the permeability, and μ is the viscosity, such that

$$u = \begin{cases} u_l & \text{in the liquid} \\ u = u_l(1-F_s) & \text{in the mushy zone} \\ 0 & \text{in the solid} \end{cases}$$

The flow in the mushy region is modeled by using a Darcy source term to modify the momentum equations such that, as the local solid fraction approaches 1, the sources dominate all other terms in the momentum equations and force the predicted velocities to approach values close to zero.

The welding problem was solved using a fixed nonuniform grid system shown in Fig. 2. All simulations were performed using an IBM RS6000 Model 530.

The assumptions made in the present analysis are as follows:

1. Even though thin plates of AISI 304 SS were used in this study, the problem was treated as three-dimensional, with only three layers through the thickness of the specimen.

2. The fluid motion in the weld pool is controlled by buoyancy, electromagnetic and surface tension forces.

3. The power distribution of the heat source is considered as Gaussian, based on available literature (Refs. 9-14).

As in the previous analyses (Ref. 18) of stationary welds, all thermophysical properties were treated as temperature dependent and are given in Fig. 3.

Boundary Conditions

The boundary conditions established were as follows:

1. At the top surface, the heat flux from the arc to the metal surface is specified as a radially symmetric Gaussian distribution.

2. The thermal boundary conditions for atmospheric cooling are formulated in terms of the convective heat transfer and radiative heat transfer. Values of 0.2 for emissivity and 84 W/m²/C for convective heat transfer coefficient were used in the calculation.

3. Along the solid-liquid interface, the conventional no-slip condition for a viscous fluid was assumed.

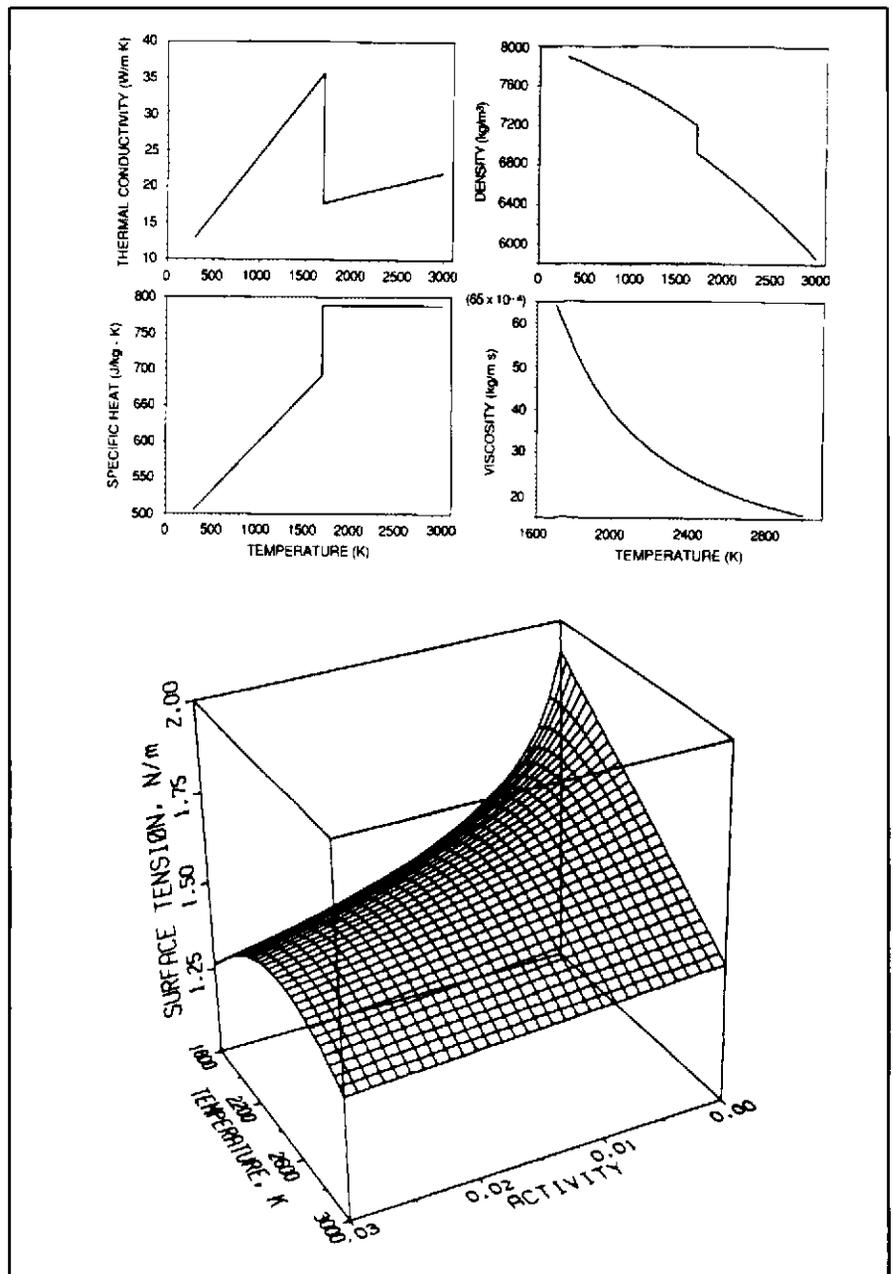


Fig. 3 — Thermophysical properties of Type 304 SS used in the present calculations.

Table 1 — Chemical Composition of 1.5-mm-Thick Type 304 Stainless Steel²³

| Composition (wt-%) | |
|--------------------|-----------|
| C | 0.06 |
| Co | 0.210 |
| Cr | 18.13 |
| Cu | 0.17 |
| Fe | remainder |
| Mn | 1.68 |
| Mo | 0.29 |
| Ni | 8.49 |
| P | 0.035 |
| S | 0.007 |
| Si | 0.55 |
| V | 0.055 |

Table 2 — Experimental and Numerical Run Conditions²³

| Case | Voltage (V) | Current (A) | Travel Speed (mm/s) |
|------|-------------|-------------|---------------------|
| 1 | 10.1 | 38 | 0.423 |
| 2 | 10.1 | 50 | 1.270 |
| 3 | 10.1 | 70 | 2.540 |
| 4 | 10.1 | 100 | 4.230 |

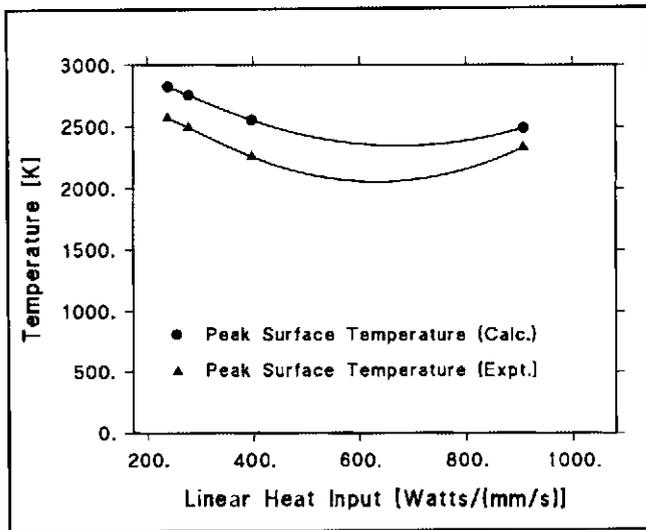


Fig. 14 — Maximum weld pool surface temperature as a function of linear heat input.

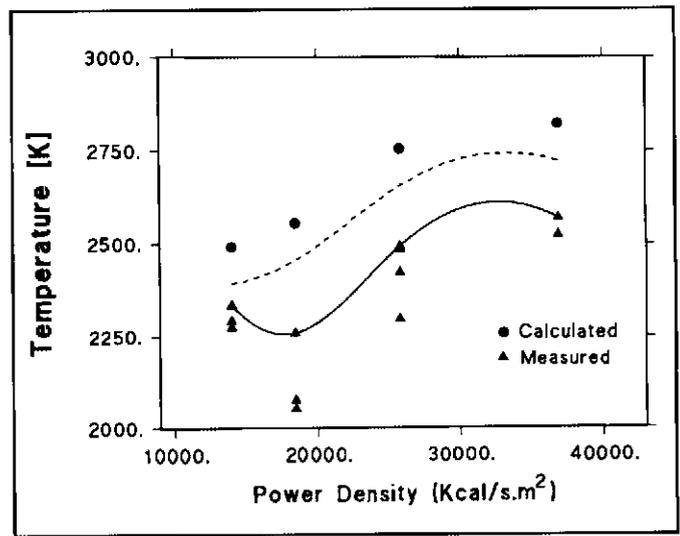


Fig. 15 — Maximum weld pool surface temperature as a function of power density.

where Q is the heat input, E the arc voltage, I the arc current and v the welding speed. Contrary to expected behavior, the weld pool peak temperatures exhibit an inverse relationship with heat input. The experimentally measured values also exhibit similar behavior with heat input. The same results are presented in Fig. 15 as a function of power density. From Fig. 15, the peak temperatures show a much better correlation with the changes in power density, suggesting that the peak surface temperature is primarily controlled by the power density. This should not be surprising, since very high peak temperatures are obtained for low power laser beam welding, where the heat inputs are considerably lower than the conventional welding process.

From Fig. 15, it is apparent that the

peak surface temperatures exhibit a non-linear relationship with welding current. In addition, the experimentally measured peak temperatures initially decreased before increasing with increasing welding current. Kraus (Ref. 25) speculated that changing weld pool convective characteristics could perhaps explain the observed deviation from expected proportional relationships. Indeed, the numerical results presented earlier show some differences in the surface flow patterns and velocities. However, there are no obvious anomalies in the convective flow that can explain the observed non-linear behavior of the peak surface temperature. It is conceivable that the observed nonlinearity reflects the dynamics between the heat input (power density) into the weld pool and the heat removal

from the weld pool due to convective and conductive heat transfer.

The calculated weld centerline surface temperatures are presented in Fig. 16 for welding speeds of 0.423 and 4.23 mm/s. In addition to the difference in peak temperatures, noted earlier, the results show significant differences in the temperature gradients for the two cases, which can influence the solidification structure within the fusion

zone. At the higher welding speed, the temperature gradient at the trailing edge of the pool is relatively shallow, which can influence the solidification structure within the fusion zone. Additionally, the relatively flat temperature gradients, which control Marangoni convection, can explain the limited flow velocities at the trailing edge of the weld pool for the higher welding speeds. The results also show that the temperature gradient (dT/dx) behind the weld pool is steeper for the weld made using the lower welding speed.

Figure 17 shows the top surface view of the weld overlaid with the calculated weld pool shape for the slowest welding speed. The macrograph shows a relatively circular weld pool similar to the predicted weld pool shape. Usually, such circular welds are associated with stationary welds. Here, in this case, the slow translation speed of the specimen with respect to the welding arc produced the circular weld pool shape. Comparison between the calculated and experimental weld pool geometry shows excellent agreement. A similar comparison was made for Case 4 and is shown in Fig. 18. The agreement in this case is not as good as Case 1 and represents the worst case of the four.

Conclusions

A multidimensional computational model was used for the analyses of heat and fluid flow during thin-plate full joint penetration welding. The model considers the solid plus liquid mushy zone as a porous media in the calculation of convective heat transfer. The computational model was used to predict the heat flow

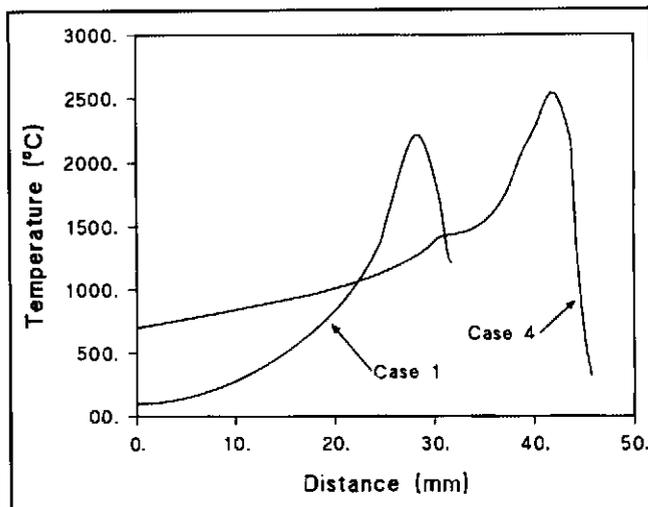


Fig. 16 — Surface temperature profiles for Case 1 and Case 4 taken from left to right through the weld centerline.

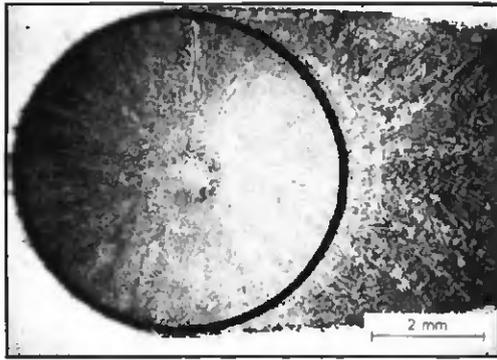


Fig. 17 — Comparison between the computed (sketch overlay) and the observed weld pool geometry for Case 1.

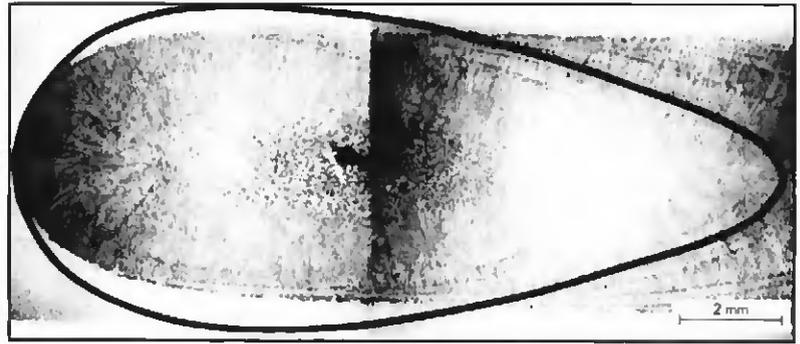


Fig. 18 — Comparison between the computed (sketch overlay) and the observed weld pool geometry for Case 4.

and fluid flow that occur during full-penetration welding of thin-plate stainless steel. The welding parameters were chosen such that the predictions of the model could be correlated with the results of an earlier experimental investigation of weld pool surface temperatures. The predictions of the weld pool surface temperatures, the weld pool size and shape were compared to the corresponding experimental measurements.

The calculated surface flows indicate that the weld pool fluid flow is controlled by the spatial variation of surface tension, particularly for thin-plate full joint penetration welds. The maximum calculated surface velocities ranged from 40 to 100 cm/s. The bulk velocities were considerably lower, ranging from 10 to 40 cm/s. The results showed that for higher welding speeds, the temperature gradients at the trailing edge of the weld pool are very small, resulting in negligible flow velocities. The relatively stagnant region at the trailing edge of the pool can have important consequences on the weld solidification structure.

In general, both computational and experimental studies indicate that the weld pool peak temperature increases with welding current. However, there does not appear to be a direct correlation between the peak surface temperature and the welding current. The calculated peak surface temperatures ranged from 2490 to 2820 K for the conditions investigated. This is in reasonable agreement with experimental measurements.

The calculated weld pool shapes were compared with the macrographs of the terminal shape of the weld pool suggesting reasonable agreement. Excellent agreement was obtained for the slow welding speed. For the highest welding speed the agreement was not as good.

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