Experiments to Simulate Effect of Marangoni Convection on Weld Pool Shape

At high Peclet numbers, the pool bottom can be flat or even convex instead of concave

BY C. LIMMANEEVICHITR AND S. KOU

ABSTRACT. Stationary welds of sodium nitrate (NaNO₃, a high-Prandtl-number material) and gallium (Ga, a low-melting-point, low-Prandtl-number material) were made with a defocused CO₂ laser beam to simulate the effect of Marangoni convection on the shape of arc weld pools without a surface-active agent. A Peclet number representing the ratio of (heat transport by convection)/(heat transport by conduction) was defined as Pe = LV/α, where L is the pool surface radius, V the maximum outward surface velocity and α the thermal diffusivity. The Ga and NaNO₃ pools represented the low and high extremes of Pe, respectively, with commonly welded metals such as aluminum, steel and stainless steel falling in between. By going to these extremes, the effect of convection on the pool shape could be much more easily understood. For Ga, Pe was low because low V (weak Marangoni convection) and high α promoted conduction down into the pool, and the resultant pool bottom was concave. For NaNO₃, however, Pe became high easily because high V (strong Marangoni convection) and very low α promoted outward convective heat transport, and the resultant pool bottom was shallow and flat. Reducing the beam diameter further increased V (even stronger Marangoni convection) and Pe. The fast outward surface flow turned and penetrated downward at the pool edge, resulting in a convex pool bottom. Both the flat and convex pool bottoms are a clear indication Marangoni convection dominated over gravity-induced buoyancy convection. It is proposed that, in the absence of both a surface-active agent and a significant electromagnetic force, the pool bottom convexity increases with increasing Pe. It was shown that, for a given material composition and welding process, the weld shape often reveals a good deal about the nature of weld pool convection.

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of the Peclet number, respectively, with weld pools of most commonly welded materials in between the two. By going to these extremes of the Prandtl and Peclet numbers, the effect of material properties and weld pool convection on the weld pool shape could be much more easily seen and understood.

Another reason for selecting NaNO₃ was because it had been used recently for flow visualization of Marangoni convection (Ref. 3). Its physical properties (Refs. 4–6) are listed in Table 1. NaNO₃ has a transmission range 0.35 to 3 µm (Ref. 7) and is, therefore, opaque to a CO₂ laser beam (10.6 µm), just as a weld pool is opaque to the heat source. The purity of the NaNO₃ used was above 99%.

The physical properties of Ga (Ref. 8) are also listed in Table 1. Semiconductor grade Ga of 99.9999% purity was used.

Samples of NaNO₃ and Ga were prepared for welding by melting and casting. The top and bottom surfaces were ground flat and cleaned before welding. The dimensions of the samples were 10 x 10 x 2 cm for NaNO₃ and 2.5 cm diameter by 1 cm height for Ga.

Welding and Pool Shape Measurement

Stationary welds were made with a defocused CO₂ laser beam, with Ar shielding to protect the pool surface from oxidation in the case of Ga. The CO₂ laser beam had a wavelength of 10.59 µm, power stability of ±5%, beam quality of M² < 1.2 and beam mode of TEM₀₀ and 90% purity (better than 90% Gaussian), where M is the magnification factor. The beam divergence was 3.2 mR. The beam power was measured with a power meter having a 0.1-W resolution, and the beam diameter was measured with a micrometer-mounted device developed recently (Ref. 3).

The welding times were 3 min for NaNO₃ and 4 min for Ga. These were sufficient for the pools to stabilize in size. The melt was decanted from the pool immediately after the CO₂ laser was turned off. In fact, there was plenty of time for decanting. Solidification of the NaNO₃ melt did not start until about 5 s after the CO₂ laser was turned off because of the rather low thermal conductivity of NaNO₃ (Table 1). The Ga melt, on the other hand, just remained undercooled at room temperature (23°C) indefinitely, i.e., for days.

The shape of the emptied pool was determined by using a digital x-y stage with a resolution of 0.01 mm and a fine-tip dial indicator with a resolution of 0.025 mm. The depth of the pool was measured every 0.25 mm along the diameter, in two directions perpendicular to each other, to determine the pool shape.

Results

NaNO₃ Pool Shapes

The shapes of the NaNO₃ pools are shown in Figs. 2 and 3. At a low power of 4.5 W and a beam diameter of 3.2 mm, the pool is small and has a concave pool bottom, as shown in Fig. 2A. The depth/width ratio is 0.184. Herein, the width refers to the diameter of the pool surface and the depth refers to the pool depth along the pool axis.

As the power is raised to 12.4 W, the pools become much wider. At the beam diameter of 5.9 mm, the pool bottom is surprisingly flat, as shown in Fig. 2B. The depth/width ratio is 0.125.

As the beam diameter is reduced from 5.9 to 1.5 mm under the same power of 12.4 W, the depth at the pool center decreases while that near the pool edge increases. As shown in Fig. 2C, this results in a peculiar pool shape, shallower at the center and deeper near the pool edge. In other words, the pool bottom has become convex toward the melt. The depth/width ratio is only 0.096.

As the power is raised from 12.4 to 232-s | AUGUST 2000
At 7.5 W of power and a 5.9-mm beam diameter, the pool becomes narrower and deeper than the wide and shallow NaNO₃ pools shown previously in Figs. 2B, 2C and 3.

At 7.5 W of power and a 5.9-mm beam diameter, the pool becomes narrower and deeper to be nearly hemispherical, as shown in Fig. 4A. The depth/width ratio is 0.389.

As the beam diameter is reduced from 5.9 to 1.5 mm under the same power of 7.5 W, the pool becomes narrower and deeper to be nearly hemispherical, as shown in Fig. 4B. The depth/width ratio is 0.496.

As the power is raised to 15 W, the pools become larger, but the characteristics of the pool shapes remain unchanged. At the beam diameter of 5.9 mm, the pool is rather concave, as shown in Fig. 5A. The depth/width ratio is 0.413.

As the beam diameter is reduced from 5.9 to 1.5 mm under the same power of 15 W, the pool once again becomes nearly hemispherical, as shown in Fig. 5B. The depth/width ratio is 0.525.

**Discussion**

**Peclet Number and Marangoni Number**

The Peclet number Pe is defined as follows (Ref. 9):

\[
Pe = \frac{LV}{\alpha} = \frac{L \rho C_p \Delta T}{k} = \frac{V \rho C_p \Delta T}{k \Delta T / L} = \frac{\text{heat transport by convection}}{\text{heat transport by conduction}} \tag{1}
\]

where \(L\) is the characteristic length, \(V\) is the characteristic velocity, \(\alpha\) is the thermal diffusivity (= \(k/\rho C_p\)), \(\rho\) is the density, \(C_p\) is the specific heat, \(k\) is the thermal conductivity and \(T\) is the temperature difference between the center and edge of the pool surface.

The purpose of using Pe here is to discuss the effect of Marangoni convection on the shape of the weld pool in the absence of a surface-active agent. As such, the characteristic length \(L\) is taken as the radius of the pool surface and the characteristic velocity \(V\) as the maximum outward surface velocity at the pool surface. In contrast, a Peclet number, based on \(L = \text{the pool depth and } V = \text{the maximum velocity in the pool, was used by Pitscheneder, et al. (Ref. 10), to explain the effect of sulfur on the shape of steel weld pools.}

The Marangoni number, which is a measure of the extent of Marangoni convection, is defined as

\[
Ma = \frac{-\gamma}{\mu \alpha} \frac{\partial T (\Delta T)}{\partial L} \tag{2}
\]

where \(\gamma\) is the temperature coefficient of surface tension, \(T\) is the temperature difference between the center and edge of the pool surface, \(\mu\) is the dynamic viscosity and \(\alpha\) is the thermal diffusivity.

When the power of the heat source is increased, \(T\) and \(\partial T / \partial L\) both increase and \(Ma\) increases. When the beam diameter is reduced, \(T\) increases very significantly, especially when the thermal conductivity is low (Ref. 3), and \(Ma\) increases very significantly. In any case, the higher \(Ma\), the stronger Marangoni convection and the higher the maximum outward surface velocity \(V\).

**NaNO₃ Pools**

For NaNO₃, the Peclet number is high for two reasons. First, the thermal conductivity \(k\) is very low (Table 1). Second, the outward maximum surface velocity \(V\) is significant and, in fact, can be rather high. Strong Marangoni convection has been observed recently by flow visualization in a simulated weld pool of NaNO₃ 10 mm in diameter, where \(Ma\) was around \(2 \times 10^4\) (Ref. 3). Since the Peclet number is high, heat transport in a NaNO₃ pool is dominated by Marangoni convection.

At a low power of 4.5 W, the pool is still small (Fig. 2A) and the Peclet number, though not small, is not yet very high in view of the small pool size and mild convection.

As the power is raised to 12.4 W and the beam becomes much wider (Fig. 2B) and Marangoni convection becomes significantly faster. Since \(L\) and \(V\) both increase, \(Pe\) increases significantly according to Equation 1. Marangoni convection dominates heat transport in the pool, and the strong outward surface flow carries heat from the laser beam to the pool edge. Since heat is transported to the pool edge more effectively and parallel to the pool surface, the resultant pool bottom is wide and flat.

Graphite powder, as a tracer to reveal convection, was introduced into the pool in a subsequent experiment. The maximum surface velocity was estimated to be about 2 cm/s from the videotape recording, based on the particle displacement measured and the 30 frames/s frame rate. From \(\alpha = 1.74 \times 10^{-3} \text{ cm}^2/\text{s}\) for NaNO₃, \(L = 5.8 \text{ mm}\) (Fig. 2B) and Equation 1, \(Pe = 670\). It is, therefore, evident Marangoni convection dominates heat transport in the pool. The error caused by the density difference between the NaNO₃ and the graphite powder can be assumed to be small.

As the power is raised further, strong convection is observed (Fig. 2C) and heat transport is no longer dominated by conduction, but by convection.
where the composition of NaNO₃ was observed no greater than 73°C because no decomposition of NaNO₃ was observed during welding. The decomposition temperature 380°C (Table 1) is only 73°C above the melting point of 307°C. It is worth mentioning that a maximum surface velocity of about 1 cm/s has been reported in the study of Marangoni convection in NaNO₃ (Ref. 6).

As the beam diameter is reduced from 5.9 to 1.5 mm under the same power of 12.4 W, Marangoni convection becomes much faster, as illustrated previously in Fig. 1B. Since V increases further, Pe also increases further. This very strong Marangoni convection forces the return flow to penetrate deeper near the pool edge and carry heat downward to the pool bottom, resulting in a convex pool bottom — Fig. 2C.

Graphite powder was again introduced into a similar pool in a subsequent experiment, and the maximum surface velocity was roughly estimated to be at least 6 cm/s from the videotape recording. From \( \alpha = 1.74 \times 10^{-3} \) cm²/s for NaNO₃, \( L = 5.5 \) mm and Equation 1, Pe = 1900. This very high Pe indicates Marangoni convection completely dominates heat transport in the pool.

Both the flat (Figs. 2B and 3A) and convex (Figs. 2C and 3B) are a clear indication that Marangoni convection dominates over gravity-induced buoyancy convection. The pool bottoms would have been concave if buoyancy convection had dominated in the pools.

Chen, et al. (Ref. 17), showed a convex pool bottom in the computer simulation of NaNO₃ welding with a moving rectangular laser beam. However, their Peclet number cannot be compared to that here since it was based on the scanning velocity of the laser beam rather than the maximum outward surface velocity, V.

**Ga Pools**

For Ga, on the other hand, the Peclet number is very low. First, its thermal conductivity k is very high (Table 1). Second, the maximum outward surface velocity V is expected to be rather small in view of the very small Ma explained below.

A thermocouple was positioned below the center of the pool surface during the laser beam welding of Ga, and a very small \( T \) of only about 3°C was measured. This very small \( T \) is not just because the thermal conductivity is very high, but also because the melting point 29.9°C is almost identical to the room temperature (23°C). Consequently, to produce a 10-mm-diameter pool in the sample, only less than 10 W is needed. Without a large \( T \) to induce significant surface tension gradients along the pool surface, there is little Marangoni convection in the pool.

From Table 1, for Ga, \( \gamma/ \) is -0.10 dyne cm⁻¹°C⁻¹, \( \mu \) is 1.94 x 10⁻² g cm⁻¹s⁻¹ and \( \alpha \) is 0.136 cm² s⁻¹. For a pool of 10 to 12 mm diameter, such as those shown in Figs. 4 and 5, \( L = 0.55 \) cm. As such, from Equation 2, \( Ma = 60 \), which is about three orders of magnitude lower than \( Ma = 2 \times 10^4 \) for NaNO₃.

Since the Peclet number is very low, heat transport in a Ga pool is dominated by conduction. The downward as well as outward heat conduction results in a concave weld pool — Fig. 4A. As the beam size is reduced under the same power, the pool becomes nearly hemispherical. This further confirms that conduction dominates heat transport in the pool. According to the theory of conduction heat transfer, a weld pool should become hemispherical in shape as the heat source shrinks in size to a point at the center of the pool surface.
Based on the above discussion, it is proposed that the pool bottom can change from concave to flat and even convex as the Peclet number increases, as illustrated in Fig. 6. The weld pool can be either stationary or traveling with respect to the workpiece. In the latter case, however, the travel speed should be significantly less than \( V \), which is usually the case, and \( V \) should be the maximum outward surface velocity in the transverse direction.

With Pe \(<1\), heat transport in the weld pool is dominated by conduction, and the pool is concave. The actual pool shape depends on the size of the heat source; with a small-size heat source, the pool is hemispherical, as illustrated in Fig. 6 (point A).

With Pe \(>>1\), on the other hand, heat transport in the weld pool is dominated by convection, and the shape of the pool bottom can change from concave to flat or even convex, as illustrated in Fig. 6 (points B–D). With stronger convection carrying more heat to the pool edge, the pool bottom becomes flat—Fig. 6 (point C). When convection gets strong enough to also carry heat downward near the pool edge, the pool bottom becomes convex—Fig. 6 (point D). The smaller the thermal diffusivity, the more significant the effect of convection on the pool shape.

**Welds in Materials of Various Prandtl Numbers**

Figure 7 is a grid showing examples of welds with a hemispherical, concave, flat or convex bottom that have been observed in materials ranging from gallium and aluminum of very low Pr (\(\approx 0.02\)) to \( Na\text{NO}_3 \) of very high Pr (\(\approx 9\)). Heat transport in the weld pool ranges from "conduction highly dominating" in the bottom-left corner of the grid to "convection highly dominating" at the top and right. These welds were made by laser beam welding (LBW), electron beam welding (EBW) or gas tungsten arc welding (GTAW), and will be called LB welds, EB welds and GTA welds, respectively. The LBW and EBW here refer to conduction-mode welding, in which the beam just deposits heat on the pool surface, as opposed to the case where the beam actually creates a vapor hole in the pool (the keyhole mode).

The interplay among many different factors determines weld pool convection. They include the power-density distribution of the heat source, the electromagnetic force in the pool, the arc plasma shear stress, the arc plasma pressure, the physical properties of the material and the surface-active agent. This interplay is sometimes too complex to analyze even with the help of computer simulation. However, in view of Fig. 7 and the observations made in the present study, it is clear that, for a given material composition and welding process, the weld shape often reveals a good deal about the nature of weld pool convection.

First, welds with a flat or convex bottom, as those in the top two rows of Fig. 7, suggest dominance of heat transport by outward surface flow induced either by Marangoni convection (in LBW and EBW) or by the arc plasma shear stress (in GTAW). Neither the electromagnetic force nor the surface-active agent plays a significant role.

Second, for metals with melting points close to the room temperature, conduction dominates heat transport in the weld pool. A more nearly hemispherical weld suggests a smaller heat source, as that in the bottom row of Fig. 7. The outward surface flow induced by Marangoni convection is too strong for commonly welded metals such as aluminum, steel and stainless steel to have a hemispherical pool. GTA, LB and EB welds of steel or stainless steel somewhat hemispherical in shape suggest dominance of heat transport by downward/inward convection induced either by the presence of a surface-active agent or by the electromagnetic force in the weld pool, or both.

Third, for commonly welded metals such as aluminum, steel and stainless steel without a surface-active agent, moderately concave welds, such as those shown in Figs. 7B, C and F, are common. Here outward surface flow induced by Marangoni convection is strong, but conduction still transports much heat down into the pool because of the low Pr.

The materials in Fig. 7 are discussed below.

**Gallium (Pr = 0.02)**

The Ga weld shown in Fig. 7A is identical to that shown previously in Fig. 4B. As already mentioned, conduction dominates heat transport in the hemispherical pool of this weld.

**Aluminum (Pr = 0.02)**

Like Ga, the thermal conductivity of aluminum is very high. Unlike Ga, however, the melting point of aluminum, \(660^\circ C\), is much higher than the room temperature, and substantial power is thus required for welding, e.g., 1500 W.
for GTAW, depending on the workpiece size. Considerable temperature gradients are thus present along the pool surface to induce strong Marangoni convection. Even so, the thermal conductivity of aluminum is so high that conduction always plays a very significant, if not dominating, role in heat transport. As such, aluminum welds made by GTAW, LBW or EBW are always concave but not hemispherical (Refs. 18–23). Figure 7B shows a concave bottom stationary weld in aluminum made by LBW (Ref. 18).

Even at very high Peclet numbers, an aluminum weld pool is still concave, rather than flat or convex. Although the outward surface flow greatly helps bring heat transport to the pool edge, this heat is still effectively dissipated by the highly conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conductive base metal instead of causing deeper melting at the pool edge like conduc...
Conclusions

1) A Peclet number has been defined as $Pe = (pool radius L) \times (maximum outward surface velocity V)/(thermal diffusivity \alpha)$ to represent the ratio of (heat transport by convection)/(heat transport by conduction) in a weld pool. The outward surface flow referred to here can be induced either by the surface-tension gradients or the arc plasma shear stress along the pool surface.

2) For the weld pools of NaNO$_3$, a high-Pr material, Pe is extremely high because of the very low thermal diffusivity $\alpha$ and strong Marangoni convection (high V), and Marangoni convection highly dominates heat transport in the weld pool.

3) Increasing the beam power, which increases Marangoni convection and the pool size, increases V, L and, hence, Pe. The heat carried outward to the pool edge by the strong outward surface flow makes a concave pool bottom wide and flat. Reducing the beam diameter, which further increases Marangoni convection, further increases V and, hence, Pe. However, the return flow penetrates the pool bottom near the pool edge and makes the flat pool bottom convex. Both the flat and convex pool bottoms indicate Marangoni convection dominates over gravity-induced buoyancy convection in the pools.

4) For the weld pools of Ga, a low-melting-point and low-Pr material, Pe is very low because of the very high thermal diffusivity $\alpha$ and weak Marangoni convection (low V), and conduction dominates heat transport in the weld pool. Heat is conducted downward as well as outward, resulting in a concave pool bottom. Reducing the beam diameter makes the Ga pool more nearly hemispherical, further confirming conduction dominates heat transport in the pool.

5) It is proposed that, in the absence of both a surface-active agent and a significant electromagnetic force, a concave pool bottom can become flat or even convex as Pe increases to reflect increasing dominance of heat transport by the outward surface flow.

6) For a given material composition and welding process, the weld shape often reveals much about the nature of weld pool convection.

Acknowledgments

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References